

CHI-SQUARE TEST (χ^2) : Test of goodness of fit

- Written as **Chi-square test** Pronounced as **Ki-Square**

χ^2

- χ^2 = Greek letter used by **Karl Pearson** in the year 1900.—to describe magnitude of difference between **Theory and Observation**.
- This test is mainly used in very **large sample size > 30**
- To test the accordance between fact and theory

- $$\chi^2 = \sum \left\{ \frac{(o-e)^2}{e} \right\}$$

- Where, O= observed freq. of the sample
- e= expected /calculated freq. of sample.
- This χ^2 value gives idea about whether the difference between observed and expected freq. is **differ significantly or not**

CHI-SQUARE TEST REQUIREMENTS

1. Quantitative data.
2. One or more categories.
3. Independent observations.
4. Theoretical freq. should not be less than 5 (at least 10).
5. Simple random sample.
6. Data in frequency form.
7. All observations must be used.

Contd..

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χ^2 - value tested with table value with d.f. (n-1).

n= frequencies of classes or Groups and not total observations.

Contingency Table and Yates Correction Factor:

Simple table with rows (**r**) and column (**c**):

Assume all cell freq. larger than 5

	Vaccinated	Not- Vaccinated	
Attacked	a	b	R1
Not-attacked	c	d	R2
	C1	C2	T

Contd....

- **Ho=Cell freq. are independent.**
- **Estimation of expected freq. of respective cell.**

	Vaccinated	Not-Vaccinated
Attacked	$\mathbf{e} = \frac{R1 * C1}{T}$	$\mathbf{f} = R1 - e$
Not-attacked	$\mathbf{g} = C1 - e$	$\mathbf{h} = C2 - f$ Or $R2 - g$

- Therefore $\mathbf{X^2} = \frac{(a-e)^2}{e} + \frac{(b-f)^2}{f} + \frac{(c-g)^2}{g} + \frac{(d-h)^2}{h}$

Contd..

- **D.F.** for Contingency table = $(r-1)(c-1) = (2-1)(2-1) = 1$
- **Conclusion:** If calculated χ^2 greater than table value of χ^2 at 1df-- **S**
- If calculated χ^2 less than table value of χ^2 at 1df-- **NS**

Yates Correction Factor:

If freq. of any cell is **5 or less than 5**, Then correction factor is needed it was suggested by **F.YATES**.

Eg

2	8	10
18	7	25
20	15	T

Add 0.5 to each cell, whose diagonal cell product is less
subtract 0.5 from each cell- which Diagonal CP is more
These are corrected freq.
Further Procedure is same for Con. Table

'F' test : ('F' Distribution)

- Used to test the **homogeneity OR Equality of VARIANCES.**
- It always estimated in terms of ratio of two variances of population keeping larger at the numerator, follows a distribution known as '**F**' **Distribution.**
- **Suppose:**
- **X_1, X_2, \dots, X_n .** Sample One with n_1 sample size & \bar{X} -mean
- **Y_1, Y_2, \dots, Y_n .** Sample two with n_2 Sample size & \bar{Y} - mean.
- **Population variance are**
- $$S_1^2 = \frac{\sum (X_i - \bar{X})^2}{n_1 - 1}, \quad S_2^2 = \frac{\sum (Y_i - \bar{Y})^2}{n_2 - 1}.$$
- **Null Hypothesis H_0 = Two samples have same variances for given population**

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- Test statistic= $F = \frac{S_1^2}{S_2^2}$, with (n_1-1) and (n_2-1) df.
- i.e F. distribution has two degrees of freedoms.
- DF for numerator – given in 1st row
- Df for denominator -- given in 1st colmn. / In 'F' table.
- **Statement of Conclusion:**

